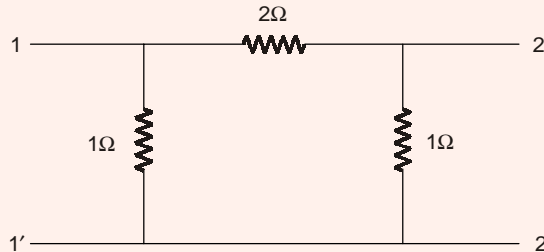


**Gate 16th Feb Evening**

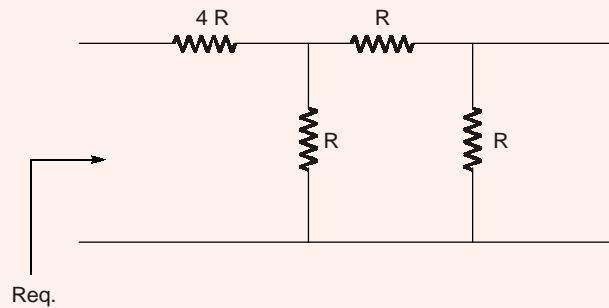
**Q.1** Find Z – parameter ( $Z_{11}, Z_{12}, Z_{21}, Z_{22}$ )



**Solution:**

$$\begin{bmatrix} \frac{3}{4} & \frac{1}{4} \\ \frac{1}{4} & \frac{3}{4} \end{bmatrix}$$

**Q.2** Find  $R_{eq}$



**Solution: (14R/3)**

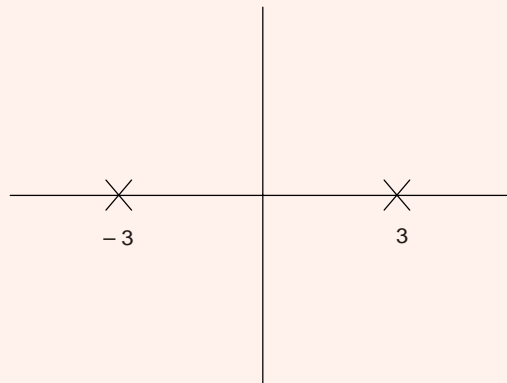
**Q.3** A stable LTI system has a transfer function  $H(S) = \frac{1}{S^2 + S - 6}$  to make this system

causal it needs to be cascaded with another LTI system having T.F.  $H_1(S)$ . Then  $H_1(S)$  is

- (a)  $S + 3$
- (b)  $S - 2$
- (c)  $S - 6$
- (d)  $S + 1$

**Solution: (b)**

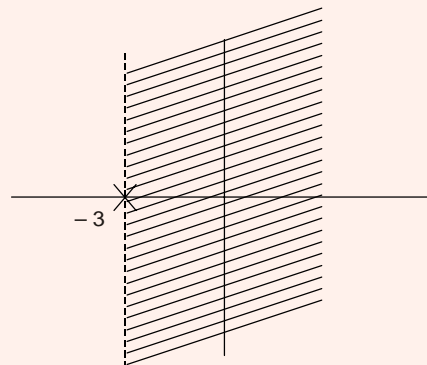
$$H(S) = \frac{1}{(S-2)(S+3)}$$



If  $H_1(S) = (S-2)$

then  $H(S)H_1(S) = \frac{1}{(S+3)}$

then



⇒ Casual

**Q.4** If sequence of 12 consecutive odd number are given, sum of first 5 number is 485. What is the sum of last 5 consecutive numbers.

**Solution: (555)**

$$n + (n + 2) + (n + 4) + (n + 6) + (n + 8) = 485$$

$$5n + 20 = 485$$

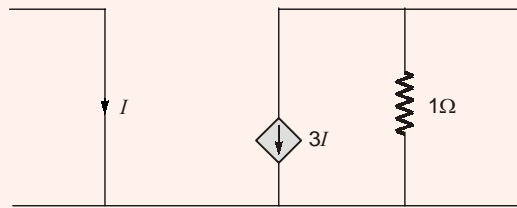
$$n = \frac{465}{5} = 93$$

$$(n + 14) + (n + 16) + (n + 18) + (n + 20) + (n + 22) = ?$$

$$= 5n + 90$$

$$= 5(93) + 90 = 90 + 450 + 15 = 555$$

**Q.5** To find: Which circuit is this ?



- (a) Voltage control, voltage source      (b) Voltage control, current source  
(c) Current control, current source      (d) Current control, voltage source

**Solution: (c)**

**Q.6** If the unilateral L.T. of signal  $f(t)$  is given as  $\frac{1}{S^2 + S + 1}$  then the Laplace transform of signal  $t.f(t)$  will be \_\_\_\_

- (a)  $\frac{1}{(S^2 + S + 1)^2}$       (b)  $\frac{1}{S^2 + S + 1}$   
(c)  $\frac{-2S + 1}{S^2 + S + 1}$       (d)  $\frac{2S + 1}{(S^2 + S + 1)^2}$

**Solution: (d)**

$$f(t) \leftrightarrow \frac{1}{(S^2 + S + 1)}$$

$$f(t) \leftrightarrow -\frac{d}{dS} \left[ \frac{1}{(S^2 + S + 1)} \right]$$

$$= +\frac{1(2S + 1)}{(S^2 + S + 1)^2} = \frac{(2S + 1)}{(S^2 + S + 1)^2}$$

**Q.7** If a signal  $x(n) = (0.5)^n u(n)$  is convolved with itself the signal obtained is  $y(n)$ , then the value of  $Y(0) =$  \_\_\_\_.

**Solution: (0)**

$$y_{(n)} = (0.5)^n u(n) \times (0.5)^n u(n)$$

$$y_{(n)} = \sum_{k=-\infty}^{\infty} (0.5)^k u(k) (0.5)^{n-k} u(n-k)$$

$$y_{(n)} = \sum_{k=0}^n (0.5)^k 1; n \geq 0 = (0.5)^0 + (0.5)^1 + \dots + (0.5)^n$$

$$y_{(n)} = \frac{((0.5)^{n+1} - 1)}{-0.5} u[n]$$

$$y_{(n)} = 2(1 - (0.5)^{n+1}) u(n)$$

$$Y(z) = \frac{2z}{z-1} - \frac{z}{z-0.5}$$

$$Y(0) = 0$$

**Q.8** If  $\left(\frac{2}{3}\right)^n u(n+3) \leftrightarrow \frac{A e^{-j6\pi f}}{1 - \frac{2}{3} e^{-j2\pi f}}$  where  $u(n)$  is unit step sequence then the value of  $A$

**Solution: (3.375)**

$$u(n) \leftrightarrow \frac{Z}{Z-1}$$

$$a^n u(n) \leftrightarrow \frac{Z}{Z-a}$$

$$\left(\frac{2}{3}\right)^{-3} \times \left(\frac{2}{3}\right)^{n+3} u(n+3) \leftrightarrow \left(\frac{2}{3}\right)^{-3} \times Z^{+3} \frac{Z}{\left(Z - \frac{2}{3}\right)}$$

Put  $Z = e^{j\omega} = e^{j2\pi f}$

$$= \left(\frac{2}{3}\right)^{-3} \frac{e^{j6\pi f} \times e^{j2\pi f}}{\left(e^{j2\pi f} - \frac{2}{3}\right)} = \frac{\left(\frac{2}{3}\right)^{-3} e^{j6\pi f} \times e^{j2\pi f}}{e^{j2\pi f} \left(1 - \frac{2}{3} e^{j2\pi f}\right)}$$

$$\therefore A = \left(\frac{2}{3}\right)^{-3} = \frac{3^3}{2^3} = \left(\frac{27}{8}\right)$$

**Q.9** If  $f(x, y) = x^n y^m = P$ . If  $x$  is doubled and  $y$  is halved, then which relation is true

(a)  $2^{n-m} P$

(b)  $2^{m-n} P$

(c)  $(m-n) P$

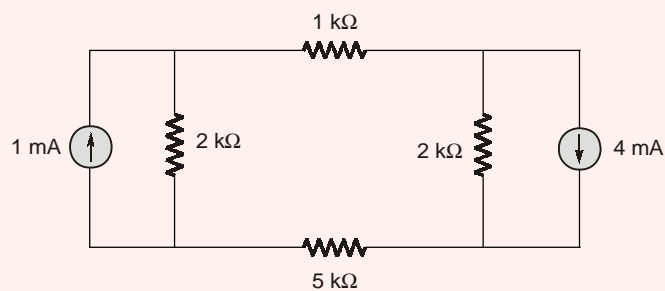
(d)  $(n-m) P$

**Solution: (a)**

$$f(x,y) = (2x)^n \times \left(\frac{y}{2}\right)^m$$

$$= 2^n \times x^n \frac{y^m}{2^m} = \frac{2^n}{2^m} x^n y^m = 2^{n-m} P$$

**Q.10** Find the magnitude of current in the 1 kΩ resistor.



**Solution: (1 Ampere)**

**Q.11** If a matrix  $\dot{x}(t) = \begin{bmatrix} 0 & 1 \\ 0 & 1 \end{bmatrix} x(t)$ . Then the state transition matrix is given as \_\_\_\_\_

(a)  $\begin{bmatrix} 1 & 0 \\ 0 & e^t \end{bmatrix}$

(b)  $\begin{bmatrix} 1 & e^t - 1 \\ 0 & 1 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 & 0 \\ te^t & 1 \end{bmatrix}$

(d)  $\begin{bmatrix} 0 & 1 \\ 1 & e^t \end{bmatrix}$

**Solution: (b)**

**Q.12** If there is a telephone station where time of incoming is independent of the time of other calls coming in past or in future. Then the pdf of this system in a fixed interval of time will be \_\_\_\_\_

(a) Poisson

(b) Gaussian

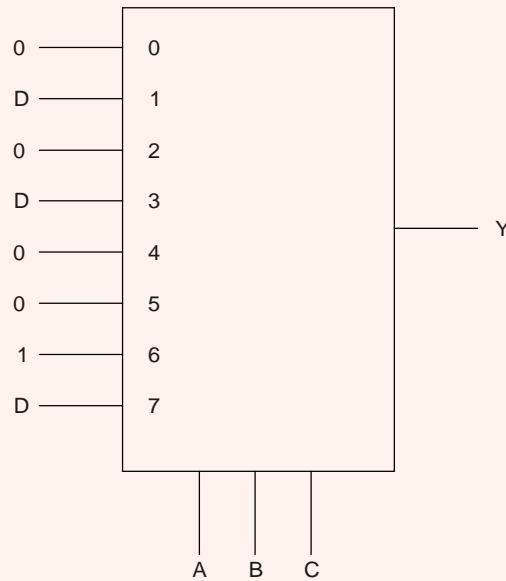
(c) Gamma

(d) Binomial

**Solution: (a)**



**Q.16** For the given  $8 \times 1$  multiplex, the output will be



**Solution:** ( $\Sigma m(3, 7, 12, 13, 15)$ )

		CD			
		00	01	11	10
AB	00	0	0	1	0
	01	0	0	1	0
	11	1	1	1	0
	10	0	0	0	0

$\Sigma m(3, 7, 12, 13, 15)$ .

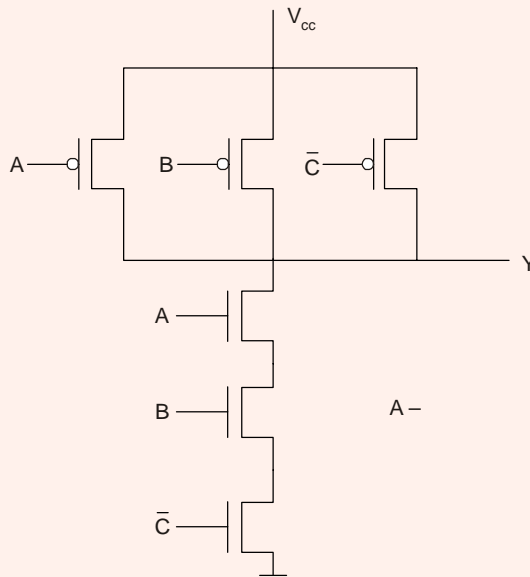
**Q.17** The equivalent output of the circuit will be

- (a)  $A' + B' + C$
- (b)  $A' B C$
- (c)  $A + B' C$
- (d) None of these

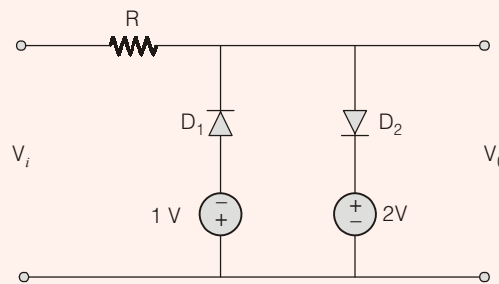
**Solution:** (a)

$$Y = \overline{A \times B \times C}$$

$$Y = (\overline{A} + B + C)$$



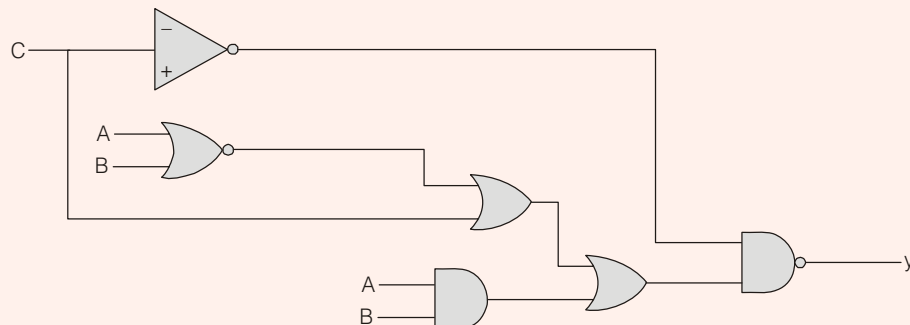
**Q.18** The output voltage  $V_0$  of the circuit shown is



- (a)  $-0.3 \text{ V} < V_0 < 1.3 \text{ V}$
- (b)  $-0.3 \text{ V} < V_0 < 2.3 \text{ V}$
- (c)  $-1.7 \text{ V} < V_0 < 2.7 \text{ V}$
- (d)  $-1.7 \text{ V} < V_0 < 1.3 \text{ V}$

**Solution: (c)**

**Q.19** If  $c = 0$  is the given logic circuit, find  $y$ .



- (a)  $\bar{A}B + A\bar{B}$
- (b)  $\bar{A} + \bar{B}$
- (c)  $A + B$
- (d)  $AB$

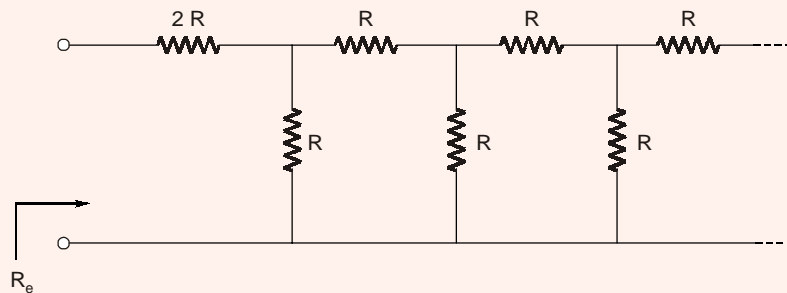


**Solution: (a)**

$$y = \overline{\overline{A + B} + AB} = \overline{A + B} \times \overline{AB}$$

$$= (\overline{A + B}) \times \overline{AB} = (A + B)(\overline{A} + \overline{B}) = \overline{A}B + A\overline{B}$$

**Q.20**  $R_e$  is \_\_\_\_\_  $k\Omega$ . (Assume  $R = 1\ k\Omega$ )

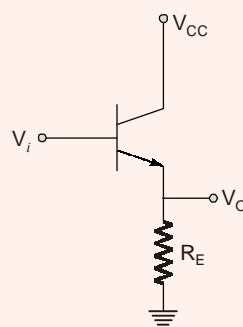


**Solution: (2.79)**

**Q.21** For an antenna radiating in free space, the Electric field at a distance of 1 km is found to be 12 mV/m. Given intrinsic impedance of free space is  $120\ \pi\ \Omega$ , magnitude of average power density due to this antenna at a distance of 2 km from the antenna is \_\_\_\_\_

**Solution: (0.047)**

**Q.22** In the above diagram what is the condition satisfied so that the gain of the above common collector amplifier is constant



- (a)  $I_C R_E \gg V_T$
- (c)  $R I_C \ll 1$

- (b)  $I_m R_E \gg 1$
- (d)  $I_C R_E \ll V_T$

**Solution: (a)**

**Q.23** Parcels from sender S to receiver R passes. Sequentially through two post offices. Each post-offices has a probability  $\frac{1}{5}$  of losing an incoming parcel, undependable of all other parcels. Given that parcel is lost, the probability that it was lost by 2<sup>nd</sup> post office is \_\_\_\_\_.

**Solution: (0.04)**

**Q.24** If the series is given as 13 M, 17 Q, 19 S, \_\_\_\_ then the next term will be

- |          |          |
|----------|----------|
| (a) 22 W | (b) 23 W |
| (c) 22 U | (d) 20 V |

**Solution: (b)**

13 M, 17 Q, 19 S, 23 W

Place apphabet

13 M  
 14 N  
 15 O  
 16 P  
 17 Q  
 18 R  
 19 S  
 20 T  
 21 U  
 22 V  
 23 W

13, 17, 19, 23 are prime numbers.

**Q.25** A person was awarded at a function, he said he was VINDICATED. Which word is nearly related to underline word.

- |               |                   |
|---------------|-------------------|
| (a) Chastened | (b) Substantiated |
| (c) Pushed    | (d) Defamed       |

**Solution: (b)**

**Q.26** A government policy was DISAGREED by the following members, which is nearly selected to underline word

- |             |              |
|-------------|--------------|
| (a) dissent | (b) decent   |
| (c) descent | (d) decadent |

**Solution: (a)**

**Q.27** If in a certain code system, “good luck” is certain “Kcldg” and “All the best” as “tsbhtl”. Then “are the exam” is written as

- (a) Mxhtr (b) Mtzhx  
 (c) cMxht (d) htcMx

**Solution: (a)**

**Q.28** The solution of the differential equation is  $\frac{d^2x}{dt^2} + \frac{2dx}{dt} + x = 0$

- (a)  $ae^{-t}$  (b)  $ate^{-t} + be^{-t} + be^{-2t}$   
 (c)  $ae^{-t} + bte^{-t}$

Where a and b are some constant

**Solution: (c)**

**Q.29** After the discussion, Tom said to me “Please revert”. He excerpts me to

- (a) retract (b) get back to him  
 (c) move in reverse (d) retreat

**Solution: (b)**

**Q.30**  $\sum_0^{\infty} \frac{1}{n!} =$  value of the sum motion equal to \_\_\_\_\_

- (a)  $2/n2$  (b) e  
 (c) 2 (d)  $\sqrt{2}$

**Solution: (b)**

■■■■